

# Tuning Control Law Gains in an Exoskeleton through Swarm Intelligence

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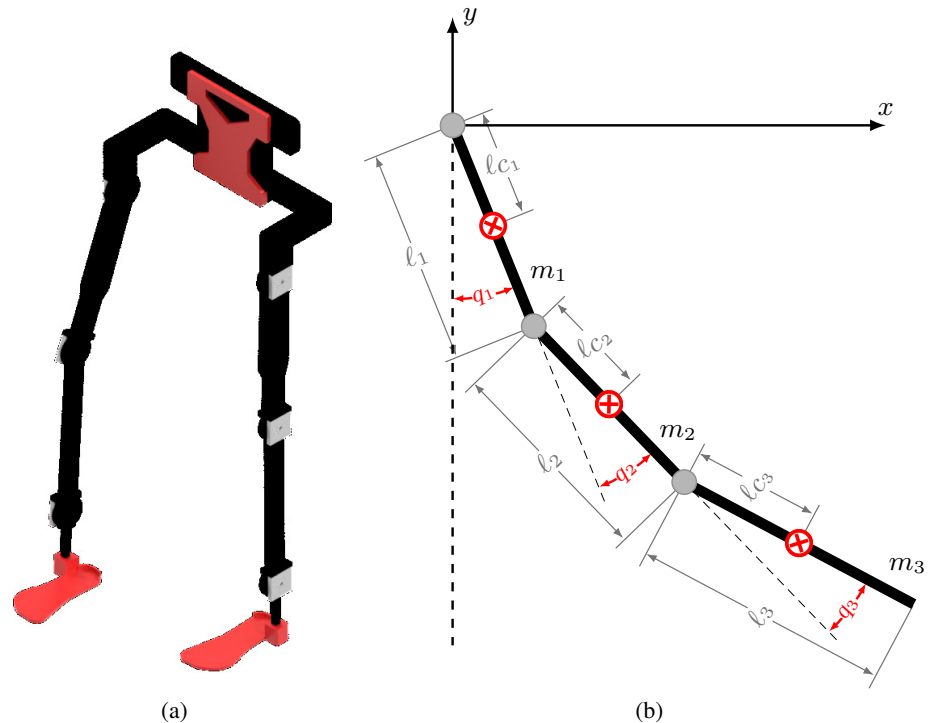
**Abstract.** Exoskeletons are mechatronic devices that can be used in physical rehabilitation programs for people who have suffered neurological injury such as ischemic or hemorrhagic brain accident. This type of injury can cause partial or total loss of mobility, so it becomes necessary to have assistive devices that support people to recover their mobility and return to their daily life. A typical problem in exoskeleton control is the adjustment of control law gains because it is challenging and lacks precision. For this reason, it seeks to know the appropriate values of the gains of a controller that generate the appropriate input torque in the exoskeleton's joints to solve the low-level control problem, managing to obtain the smallest possible error between the input reference path and the current angular position. To know the appropriate parameters, it is assumed that with the use of optimization tools such as evolutionary computing algorithms or collective intelligence the error signal in a multiple-joint structure, such as the exoskeleton, could be minimized. Comparison between heuristic and intelligent methods shows that objective function could be minimized to obtain best gains values, therefore, intelligent method calculates better performance values in terms of angular position error, so considering the calculated gains, the low-level control has been improved to accomplish with trajectory tracking problem.

**Keywords:** Exoskeleton, mechatronic assistive device, PID intelligent tuning, particle swarm optimization, integral squared error.

## 1 Introduction

As per the World Health Organization (WHO), more than 15% of people worldwide experiences some form of disability [5]. In the year 2010, in the United States exclusively, approximately 30.6 million individuals faced disability-related challenges with their mobility, such as having trouble in walking, climbing stairs or descending them, assistance of a wheeled chair, zimmer frame, cane or walking sticks [3].

Talking about the European Union in the year of 2011, is mentioned that there are over 11,000 people with walking disabilities [6]. Based on the National Health and Nutrition Survey of 2012, at a nationwide scale, approximately 4.9% of males and 5.8% of females (equivalent to around 2.5 million and 3 million individuals, respectively) were documented to have a disability affecting their mobility or ability to walk [8].



**Fig. 1.** (a) Mechanical design of a 6 DOF exoskeleton. (b) Rigid body diagram considered for Euler-Lagrange mathematical modelling.

In the specific case of disabilities in the lower limbs, they may originate from congenital anomalies [24], chronic conditions [4], or injuries [23, 12]. Overall statistics show that disabilities related to neuromuscular pathologies of lower limbs are prevalent. Among these medical conditions is the occurrence of an ischemic or hemorrhagic incident, commonly referred to as a stroke, which occurs when a thrombus obstructs or constricts an artery responsible for supplying blood to the brain.

Some lifestyle related risk factors are being overweight or obese, physically inactive or drinking alcoholic beverages in excess, meanwhile, medical risk factors encompass elevated blood pressure, high cholesterol, diabetes, among other conditions, with one of the prevailing complications being paralysis or impaired muscle movement [14]. To improve the quality of life of a person with such a complication, it is necessary to provide treatment options and therapies so that affected patients can successfully reintegrate into their daily activities.

One tool that may be useful in physical rehabilitation programmes is exoskeletons [19]. The development of mechatronic exoskeletons involves at least the following stages: mechanical design (number of degrees of freedom, kinematic and dynamic capabilities, mechanical constraints), instrumentation (sensor selection, actuators, processing system), control (control modules or algorithms defining the automatic behaviour of the device) [21].

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**Algorithm 1** PSO pseudocode.

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1: Generate population
2: for  $t = 1$  : last generation do
3:   for  $i = 1$  : population size do
4:     if  $f(X_{i,k}(t)) < f(p_i(t))$  then  $f(p_i(t)) = f(X_{i,k}(t))$ 
5:        $f(G_{\text{best}}(t)) = \min(f(p_i(t)))$ 
6:     end if
7:     for  $k = 1$  to problem dimension do
8:        $V_{i,k}(t+1) = wV_{i,k}(t) + c_1 r_1(P_{\text{best}} - X_{i,k}(t)) + c_2 r_2(G_{\text{best}} - X_{i,k}(t))$ 
9:        $X_{i,k}(t+1) = X_{i,k}(t) + V_{i,k}(t+1)$ 
10:      if  $V_{i,k}(t+1) > v_{\text{max}}$  then  $V_{i,k}(t+1) = v_{\text{max}}$ 
11:      else if  $V_{i,k}(t+1) < v_{\text{min}}$  then  $V_{i,k}(t+1) = v_{\text{min}}$ 
12:      end if
13:      if  $X_{i,k}(t+1) > x_{\text{max}}$  then  $X_{i,k}(t+1) = x_{\text{max}}$ 
14:      else if  $X_{i,k}(t+1) < x_{\text{min}}$  then  $X_{i,k}(t+1) = x_{\text{min}}$ 
15:      end if
16:    end for
17:  end for
18: end for

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There is currently a wide variety of exoskeleton concept tests, including some commercial developments, such as the Indego, ReWalk, HAL, Exo-H3 and Ekso GT [19]. Commonly developments include four acting degrees of freedom (hip and knee) [10]. This imposes the challenge of extending the mechanical design to have exoskeletons that consider motion acting on the three main joints of the lower extremities, namely: hip, knee and ankle.

There are direct antecedents on the design and control of exoskeletons as reported in [22] and [2]; however, there are still many questions to be solved in terms of energy modulation of such devices. When discussing exoskeleton control strategies, it is essential to consider the three distinct levels involved: high level, medium level, and low level.

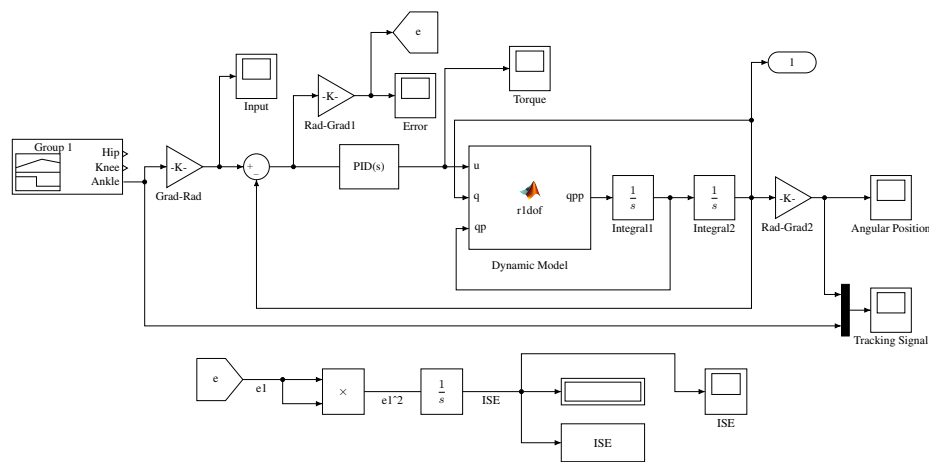
The high-level control pertains to land identification, where the focus lies on identifying and assessing the terrain. The medium-level control is concerned with the operation mode, determining the appropriate mode of operation based on the given circumstances. Lastly, the low-level control aims to achieve the desired torque or position for the articulations involved [1].

This research work develops the dynamic model from the Euler Lagrange equations based in an exoeskeleton model and proposes a PID controller [16] tuned using optimization tools such as swarm intelligence algorithms [20] applied to finding the appropriate gains to solve the low level control problem.

Comparison between two methods shows that objective function could be minimized to obtain best gains values, therefore, intelligent method calculates better performance values in terms of angular position error, so considering the calculated gains, the low-level control has been improved to accomplish with trajectory tracking problem.

**Table 1.** Dynamic model parameters.

Parameter	Value
Mass ( $m$ )	5
Length ( $\ell$ )	0.45
Center of mass length ( $\ell_c$ )	0.01
Inertia moment ( $I$ )	0.1595
Viscous friction coefficient ( $b$ )	0.17
Coulomb friction coefficient ( $f_c$ )	0.45
Gravity ( $g$ )	9.8



**Fig. 2.** Diagram developed in MATLAB-Simulink to obtain the trajectory tracking, trajectory error and torque from the three different input signals.

## 2 Exoskeleton Mathematical Model

The mechanical design of the exoskeleton seeks to reproduce the joint movement of the lower extremities of the human body as shown in Figure 1a. The resulting mechanism is planar and its movement can be mathematically modeled with the Euler-Lagrange methodology for planar robots.

Because the mechanism reproduces the movement of the lower limb extremities, the model is proposed as a pair of open chains of three degrees of freedom each as shown in Figure 1b. This section describes the methodology for obtaining the dynamic model of one of the open chains, assuming it is the same methodology for two chains.

### 2.1 Euler-Lagrange Equations

The Euler Lagrange equations describes the dynamics of the articular positions and velocities of a mechanical system and is given by [9]:

$$\tau = \frac{d}{dt} \left[ \frac{\partial L(q, \dot{q})}{\partial \dot{q}} \right] - \left[ \frac{\partial L(q, \dot{q})}{\partial q} \right] + f_f(f_e, \dot{q}), \quad (1)$$

**Table 2.** PSO parameters.

Parameter	Value
Cognitive factor ( $c_1$ )	1.2
Social factor ( $c_2$ )	0.12
Inertia weight ( $w$ )	0.9
No. of particles ( $n$ )	30
Max iteration	30
Dimension (dim)	3
Random values ( $r_1, r_2$ )	rand(dim, n)
Initial conditions ( $K_p, K_i, K_d$ )	25, 5, 5

**Table 3.** Objective function values considering heuristic method.

Parameter	Value
Hip	11.13
Knee	15.33
Ankle	9.936

where,  $\tau = [\tau_1 \ \tau_2 \ \tau_3]^T$  is the joint pairs vector,  $q = [q_1 \ q_2 \ q_3]^T$  is the angular positions vector,  $\dot{q} = [\dot{q}_1 \ \dot{q}_2 \ \dot{q}_3]^T$  is the angular velocities vector,  $L(q, \dot{q})$  is the Lagrangian function and  $f_f(f_e, \dot{q})$  is a friction function. The Lagrangian function is given by the following:

$$L(q, \dot{q}) = K_i(q, \dot{q}) - U_i(q), \quad i = 1, 2, 3, \quad (2)$$

where,  $K_i(q, \dot{q})$  is the kinetic energy and  $U_i(q)$  is the potential energy. The kinetic energy of each bond of a mechanism is defined as:

$$K_i(q, \dot{q}) = \frac{1}{2} [m_i v_i^T v_i + I_i \dot{q}^2], \quad (3)$$

where,  $m_i$  is the mass of the link to be analyzed,  $v_i$  is the linear speed of the link and  $I_i$  is the moment of inertia tensor of the link. On the other hand, potential energy is defined as:

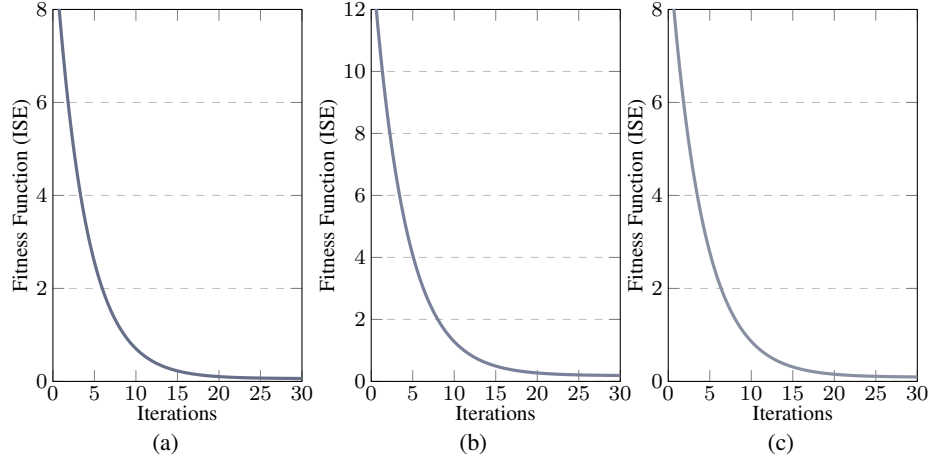
$$U_i(q) = m_i g h_i, \quad (4)$$

where,  $g$  is the ground gravity constant and  $h_i$  is the current height of the link with respect to the ground. To construct the equation of motion the equations (3) and (4) are replaced in the equation (2), the corresponding derivatives are calculated and thus the equation (1) is obtained.

Friction terms are not considered for this problem. A common way to represent the result of evaluating equation (1) is the so-called dynamic model in matrix form defined as [17]:

$$\tau = M(q)\ddot{q} + C(q, \dot{q}) \dot{q} + G(q), \quad (5)$$

where,  $\ddot{q} = [\ddot{q}_1 \ \ddot{q}_2 \ \ddot{q}_3]^T$  refers to the vector of angular accelerations,  $M(q)$  is the inertial matrix,  $C(q, \dot{q})$  is the matrix of centripetal forces and the gravity pair vector,



**Fig. 3.** (a) Fitness objective function for the hip trajectory, (b) fitness objective function for the knee trajectory (c) fitness objective function for the ankle trajectory.

denoted as  $G(q)$ :

$$M(q) = \begin{bmatrix} M_{11} & M_{12} & M_{13} \\ M_{21} & M_{22} & M_{23} \\ M_{31} & M_{32} & M_{33} \end{bmatrix}, \quad (6)$$

where:

$$\begin{aligned} M_{11} &= I_1 + I_2 + I_3 + \ell_1^2 m_2 + \ell_1^2 m_3 + \ell_2^2 m_3 + \ell_{c_1}^2 m_1 + \ell_{c_2}^2 m_2 + \ell_{c_3}^2 m_3 + 2 \ell_1 \ell_{c_3} m_3 \\ &\quad \cos(q_2 + q_3) + 2 \ell_1 \ell_2 m_3 \cos(q_2) + 2 \ell_1 \ell_{c_2} m_2 \cos(q_2) + 2 \ell_2 \ell_{c_3} m_3 \cos(q_3), \\ M_{12} &= I_2 + I_3 + m_3 \left( \ell_2^2 + 2 \ell_2 \ell_{c_3} \cos(q_3) + \ell_1 \ell_2 \cos(q_2) + \ell_{c_3}^2 + \ell_1 \ell_{c_3} \cos(q_2 + q_3) \right) + \\ &\quad \ell_{c_2} m_2 \left( \ell_{c_2} + \ell_1 \cos(q_2) \right), \\ M_{13} &= I_3 + \ell_{c_3} m_3 \left( \ell_{c_3} + \ell_1 \cos(q_2 + q_3) + \ell_2 \cos(q_3) \right), \\ M_{21} &= I_2 + I_3 + m_3 \left( \ell_2^2 + 2 \ell_2 \ell_{c_3} \cos(q_3) + \ell_1 \ell_2 \cos(q_2) + \ell_{c_3}^2 + \ell_1 \ell_{c_3} \cos(q_2 + q_3) \right) + \\ &\quad \ell_{c_2} m_2 \left( \ell_{c_2} + \ell_1 \cos(q_2) \right), \\ M_{22} &= I_2 + I_3 + \ell_{c_2}^2 m_2 + m_3 \left( \ell_2^2 + 2 \ell_2 \ell_{c_3} \cos(q_3) + \ell_{c_3}^2 \right), \\ M_{23} &= I_3 + m_3 \left( \ell_{c_3}^2 + \ell_2 \ell_{c_3} \cos(q_3) \right), \\ M_{31} &= I_3 + \ell_{c_3} m_3 \left( \ell_{c_3} + \ell_1 \cos(q_2 + q_3) + \ell_2 \cos(q_3) \right), \\ M_{32} &= I_3 + m_3 \left( \ell_{c_3}^2 + \ell_2 \ell_{c_3} \cos(q_3) \right), \\ M_{33} &= I_3 + \ell_{c_3}^2 m_3. \end{aligned}$$

$$C(q, \dot{q}) = \begin{bmatrix} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \end{bmatrix}, \quad (7)$$

where:

$$C_{11} = 0,$$

$$C_{12} = -2 \ell_1 \dot{q}_1 \left( \ell_2 m_3 \text{Sen}(q_2) + \ell_{c_2} m_2 \text{Sen}(q_2) + \ell_{c_3} m_3 \text{Sen}(q_2 + q_3) \right) - \ell_1 \dot{q}_2 \left( \ell_2 m_3 \text{Sen}(q_2) + \ell_{c_2} m_2 \text{Sen}(q_2) + \ell_{c_3} m_3 \text{Sen}(q_2 + q_3) \right) - \ell_1 \ell_{c_3} m_3 \dot{q}_3 \text{Sen}(q_2 + q_3),$$

$$C_{13} = -\dot{q}_1 \left( 2 \ell_1 \ell_{c_3} m_3 \text{Sen}(q_2 + q_3) + 2 \ell_2 \ell_{c_3} m_3 \text{Sen}(q_3) \right) - m_3 \dot{q}_2 \left( 2 \ell_2 \ell_{c_3} \text{Sen}(q_3) + \ell_1 \ell_{c_3} \text{Sen}(q_2 + q_3) \right) - \ell_{c_3} m_3 \dot{q}_3 \left( \ell_1 \text{Sen}(q_2 + q_3) + \ell_2 \text{Sen}(q_3) \right),$$

$$C_{21} = 0,$$

$$C_{22} = -\dot{q}_1 \left( m_3 \left( \ell_1 \ell_2 \text{Sen}(q_2) + \ell_1 \ell_{c_3} \text{Sen}(q_2 + q_3) \right) + \ell_1 \ell_{c_2} m_2 \text{Sen}(q_2) \right),$$

$$C_{23} = -\ell_{c_3} m_3 \left( 2 \ell_2 \dot{q}_1 \text{Sen}(q_3) + 2 \ell_2 \dot{q}_2 \text{Sen}(q_3) + \ell_2 \dot{q}_3 \text{Sen}(q_3) + \ell_1 \dot{q}_1 \text{Sen}(q_2 + q_3) \right),$$

$$C_{31} = 0,$$

$$C_{32} = -\ell_1 \ell_{c_3} m_3 \dot{q}_1 \text{Sen}(q_2 + q_3),$$

$$C_{33} = -\ell_{c_3} m_3 \dot{q}_1 \left( \ell_1 \text{Sen}(q_2 + q_3) + \ell_2 \text{Sen}(q_3) \right) - \ell_2 \ell_{c_3} m_3 \dot{q}_2 \text{Sen}(q_3).$$

$$G(q) = \begin{bmatrix} G_1 \\ G_2 \\ G_3 \end{bmatrix}, \quad (8)$$

where:

$$G_1 = g m_3 \left( \ell_2 \text{Sen}(q_1 + q_2) + \ell_1 \text{Sen}(q_1) + \ell_{c_3} \text{Sen}(q_1 + q_2 + q_3) \right) + g m_2 \left( \ell_{c_2} \text{Sen}(q_1 + q_2) + \ell_1 \text{Sen}(q_1) \right) + 2 g \ell_{c_1} m_1 \text{Sen}(q_1),$$

$$G_2 = g m_3 \left( \ell_2 \text{Sen}(q_1 + q_2) + \ell_{c_3} \text{Sen}(q_1 + q_2 + q_3) \right) + g \ell_{c_2} m_2 \text{Sen}(q_1 + q_2),$$

$$G_3 = g \ell_{c_3} m_3 \text{Sen}(q_1 + q_2 + q_3).$$

### 3 Exoskeleton Control System

Dynamic models can be examined through the approach of both linear and nonlinear systems. In the context of control system tuning, a heuristic approach is often employed for linear systems, while intelligent algorithms are typically harnessed when dealing with nonlinear systems. The heuristic tuning method in control is based on empirically adjusting the parameters of a controller rather than using a purely analytical or theoretical approach.

**Table 4.** Objective function values considering intelligent method.

Parameter	Value
Hip	0.1074
Knee	0.2328
Ankle	0.1341

This approach is used when the system is complex and optimal controller parameter values cannot be calculated directly. Intelligent tuning methods for control are based on the use of artificial intelligence (AI) or machine learning (ML) techniques to automatically adjust and optimize the parameters of a control system [25]. To illustrate the operation of the proposed design in the reproduction of lower limb movements, it is proposed to solve a trajectory tracking control problem using a PID control scheme that calculates the torque for each of the exoskeleton joints.

### 3.1 Control Scheme

It is considered  $q_d = [q_{d1} \ q_{d2} \ q_{d3}]^T$  as the reference trajectories to be reproduced on each of the legs of the exoskeleton, then considering the angular position  $q = [q_1 \ q_2 \ q_3]^T$ , the position error is defined as the vector:

$$e(t) = \begin{bmatrix} q_{d1}(t) - q_1(t) \\ q_{d2}(t) - q_2(t) \\ q_{d3}(t) - q_3(t) \end{bmatrix}, \quad (9)$$

From the error vector  $e(t)$ , the PID law control [16] is defined as:

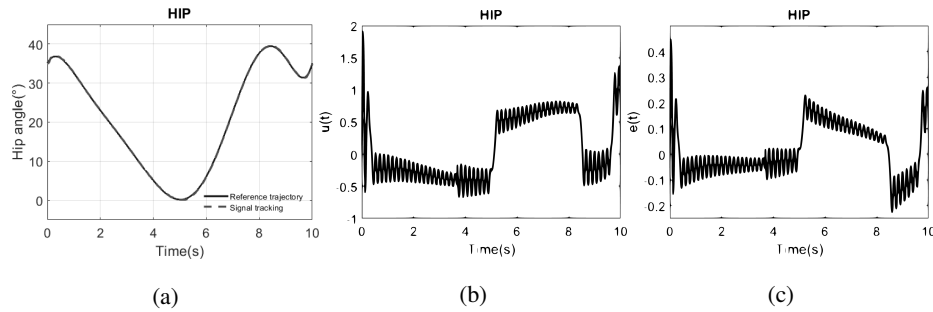
$$\tau = K_p e(t) + K_v \dot{e}(t) + K_i \int_0^t e(t) dt, \quad (10)$$

where  $\tau = [\tau_1 \ \tau_2 \ \tau_3]^T$  are the pairs in the three joints of each leg and  $K_p$ ,  $K_v$  y  $K_i \in R^{3 \times 3}$  are the defined positive gain matrices, called proportional, derivative and integral gain, respectively. To solve the control problem, the reference trajectories  $q_d$  are then required. In this work, the data reported in [18] about the angular positions of the hip, knee, and ankle (both legs) in study subjects who performed walking activities were used as reference trajectories.

### 3.2 Optimization of the Controller's Gains

The numeric value of the gain matrices is calculated based on Particle Swarm Optimization algorithm (PSO), such that the closed-loop system response converges to the proposed input reference. PSO is an optimization technique inspired by the cooperative patterns observed in nature, such as the flocking of birds and the schooling of fish.





**Fig. 4.** (a) Trajectory tracking signal, (b) input torque and (c) trajectory error signal, of the hip joint.

**Table 5.** Calculated gains from PSO algorithm.

Joint	$K_p$	$K_i$	$K_d$
Hip	240.9220	122.7799	23.8527
Knee	210.6642	131.6928	3.45810
Ankle	241.7013	27.69170	17.6263

It is a metaheuristic approach that exhibits several advantages: PSO necessitates minimal or no assumptions regarding the optimization problem at hand, it does not depend on problem differentiability, and it can explore vast solution spaces. These attributes make PSO a potent tool for tackling multidimensional and intricate optimization problems.

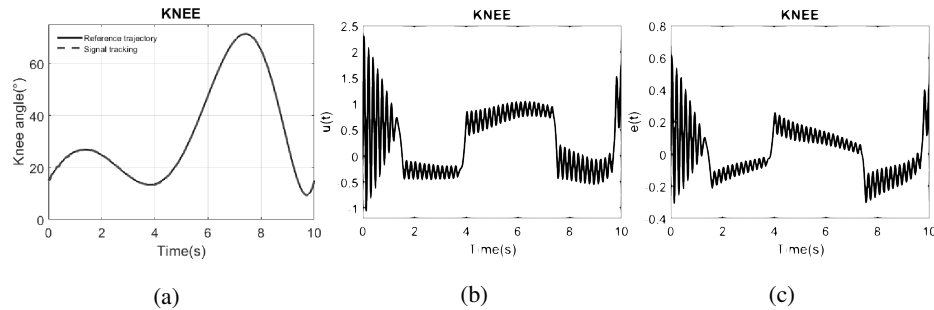
Within the framework of the PSO algorithm, the particles, representing potential solutions, navigate through the search space by aligning their movements with the current optimal particle. Essentially, at the  $k$ -th iteration, each particle  $p_i$  in the swarm possesses two attributes: its position denoted as  $X(t)$  and its velocity denoted as  $V(t)$ .

The particle's motion is determined in terms of velocity that combines the influence of its own best position  $P_{best}$  and the collective best position of the complete swarm  $G_{best}$  inside the exploration domain:

$$V(t + 1) = w V(t) + c_1 r_1 (P_{best} - X(t)) + c_2 r_2 (G_{best} - X(t)), \quad (11)$$

$$X(t + 1) = X(t) + V(t + 1). \quad (12)$$

More precisely, the speed of each individual particle undergoes an update using Equation (11). In this equation, the cognitive and social learning coefficients are represented by  $c_1$  and  $c_2$ , respectively. The prescribed inertia weight is represented by  $w$ , while  $r_1$  and  $r_2$  denote random numbers generated within the range of 0 and 1 during each iteration. The particle's position can be updated using Equation (12). The iteration process concludes either when the predetermined number of iterations is attained or when the objective function  $f(t)$  reaches a critical value [11].



**Fig. 5.** (a) Trajectory tracking signal, (b) input torque and (c) trajectory error signal, of the knee joint.

### 3.3 Objective Functions

Selecting the objective functions to assess the fitness of each particle stands as a pivotal step in the implementation of PSO [15]. Among the objective functions commonly employed are the Mean Squared Error (MSE), the Integral of Time multiplied by Absolute Error (ITAE), the Integral of Absolute Error (IAE), and the Integral of Squared Error (ISE) [7]. In this study, the objective function employed is ISE due to its minimal energy consumption in the context of energy control [13] and is described by the following equation:

$$ISE = \int_0^t e^2(t) dt, \quad (13)$$

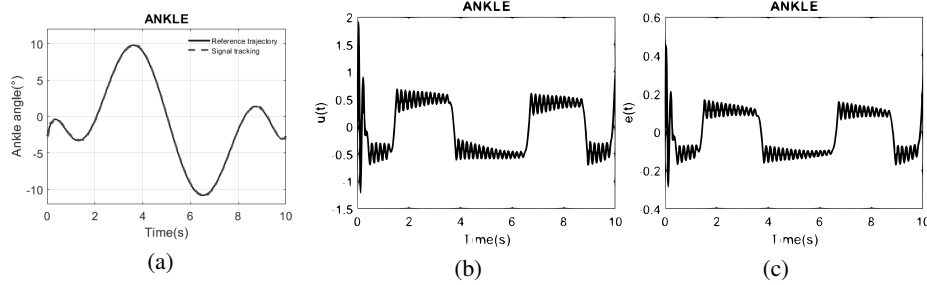
where  $e(t)$  is the error signal and is based in Equation (9).

## 4 Experiment Design

The simulation of the exoskeleton experiment as shown in Figure 2, is developed in Matlab-Simulink considering a mathematical model of 1 DOF, the trajectory input signals, the PID control system and the PSO intelligent tuning method using ISE as objective function. The decision variables considered in the PSO algorithm are based on the minimization of the objective function ISE, when PSO finds a better population of particles, the value of the objective function is updated until the end of the simulation by restricting the iterations.

It is well known that the PID control law does not generate an equilibrium point of the closed-loop system with global asymptotic stability characteristics, it only has local asymptotic stability as long as the gains are positive defined, therefore, the algorithm has the constraint of only looking for positive gain values such that the closed-loop system response converges to the reference trajectories.

It is important to mention that ISE function global minimum value is 0. Thus, PSO algorithm works to optimize the objective function to zero that is equals to calculate a minimum trajectory tracking error.



**Fig. 6.** (a) Trajectory tracking signal, (b) input torque and (c) trajectory error signal, of the ankle joint.

Then, the optimization problem can be defined as follows:

$$e(t) = q_{di}(t) - q_i(t), \text{ such that, } ISE = \int_0^t e^2(t) dt = 0 \text{ (Global minimum), } \quad (14)$$

considering that,  $K_p, K_i$  and  $K_d \in R^+$ . Thus:

$$\tau = K_p e(t) + K_v \dot{e}(t) + K_i \int_0^t e(t) dt, \text{ converge to trajectory signals. } \quad (15)$$

As mentioned in subsection 3.1, the trajectory input signals was taken from [18] and the acceleration of the 1 DOF dynamical model is calculated as follow:

$$\ddot{q} = \frac{[\tau - m g \ell_c \text{Sen } q - b \dot{q} - f_c \text{signo}(\dot{q})]}{[\ell_c^2 + I]}. \quad (16)$$

The parameters used to simulate the dynamic model are shown in Table 1. The experiment parameters to simulate the PSO are presented in Table 2 and as mentioned in subsection 3.3, ISE is used as objective function based on the error signal from the closed-loop system. Table 3 shows the objective function calculated values based on the heuristic method. Also, gain values from heuristic method were used as initial conditions for the intelligent method. Objective function for the three joints during the iterative process of the intelligent method is presented in Figure 3 and the calculated values are presented in Table 4.

## 5 Results

Having considered the previous work, this section presents the results of the dynamic model from the Euler Lagrange motion equations and the solution of the trajectory tracking control problem using a PID schema based in PSO to find the best gain values based on ISE objective function. The calculated gain values are presented in Table 5. The results of tracking, input torque and error for joints are shown in Figures 4, 5 and 6.

## 6 Conclusions

Utilizing conventional methods to implement a controller for a multiple joint structure proves to be challenging and lacks precision. Integrating intelligent swarm optimization techniques, such as PSO, presents a viable approach for fine-tuning PID controllers. As mentioned in subsection 3.3, there is a range of objective functions available for consideration.

However, within the context of energy control, ISE was selected as the objective function to be optimized by the PSO algorithm for tuning the PID controller gains. Results shows that the tuned controller scheme generate adequate torques to accomplish the trajectory tracking problem. The intelligent method calculates better performance values in terms of angular position error, so considering the generated gains, the low-level control was improved compared with the heuristic method.

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